



Band Filling Control of the Dzyaloshinskii-Moriya Interaction in Weakly Ferromagnetic Insulators

G. Beutier,^{1,*} S. P. Collins,² O. V. Dimitrova,³ V. E. Dmitrienko,⁴ M. I. Katsnelson,^{5,6} Y. O. Kvashnin,⁷
A. I. Lichtenstein,^{6,8} V. V. Mazurenko,⁶ A. G. A. Nisbet,² E. N. Ovchinnikova,³ and D. Pincini^{9,2}

¹Univ. Grenoble Alpes, CNRS, Grenoble INP, SIMaP, F-38000 Grenoble, France

²Diamond Light Source Ltd., Diamond House, Harwell Science and Innovation Campus, Didcot,
Oxfordshire OX11 0DE, United Kingdom

³M. V. Lomonosov Moscow State University, Leninskie Gory, Moscow 119991, Russia

⁴A. V. Shubnikov Institute of Crystallography, FSRC “Crystallography and Photonics” RAS, Moscow 119333, Russia

⁵Radboud University Nijmegen, Institute for Molecules and Materials, Heyendaalseweg 135, NL-6525 AJ Nijmegen, The Netherlands

⁶Department of Theoretical Physics and Applied Mathematics, Ural Federal University, Mira 19, 620002 Ekaterinburg, Russia

⁷Department of Physics and Astronomy, Division of Materials Theory, Uppsala University, Box 516, SE-75120 Uppsala, Sweden

⁸I. Institut für Theoretische Physik, Universität Hamburg, Jungiusstraße 9, D-20355 Hamburg, Germany

⁹London Centre for Nanotechnology and Department of Physics and Astronomy, University College London,
London WC1E 6BT, United Kingdom

(Received 7 May 2017; published 19 October 2017)

We observe and explain theoretically a dramatic evolution of the Dzyaloshinskii-Moriya interaction (DMI) in the series of isostructural weak ferromagnets, MnCO_3 , FeBO_3 , CoCO_3 , and NiCO_3 . The sign of the interaction is encoded in the phase of the x -ray magnetic diffraction amplitude, observed through interference with resonant quadrupole scattering. We find very good quantitative agreement with first-principles electronic structure calculations, reproducing both sign and magnitude through the series, and propose a simplified “toy model” to explain the change in sign with $3d$ shell filling. The model gives insight into the evolution of the DMI in Mott and charge transfer insulators.

DOI: 10.1103/PhysRevLett.119.167201

Introduction.—The Dzyaloshinskii-Moriya interaction (DMI) appears in magnetic materials with, at least locally, broken inversion symmetry. It leads to an exchange energy that scales with the vector product of spins $\mathbf{S}_1 \times \mathbf{S}_2$ and is thus antisymmetric with respect to interchange of the spins, favoring noncollinear order. First introduced to explain the canting of moments in weak ferromagnets [1], with a microscopic origin in spin-orbit coupling (SOC) [2,3], the DMI has recently been shown to be responsible for the stabilization of various exotic noncollinear magnetic ground states, such as spin spirals [4] and Skyrmions [5–7]. Such magnetic orders are of particular interest from both fundamental and applied points of view. For instance, Skyrmions are topologically protected states, which makes them promising for novel spintronic applications. DMI is an important ingredient in multiferroics with spiral magnetic order, where it is thought to promote an electric polarization either by polarizing electronic orbitals [8] or by inducing atomic displacements [9]. DMI stabilizes chiral domain walls, which can be driven by current rather

than magnetic field [10,11]. Also, they can be used for manipulation of spin wave currents (“magnon transistor”) [11]. The possibility to control and change the sign of the DMI in magnetic materials is an essential step towards finding suitable materials for spintronics applications. Up to date such manipulation has been experimentally realized for the isostructural $B20$ metallic alloys $\text{Fe}_{1-x}\text{Co}_x\text{Si}$ [12], $\text{Mn}_{1-x}\text{Fe}_x\text{Ge}$ [13], and $\text{Fe}_{1-x}\text{Co}_x\text{Ge}$ [14] demonstrating a very complex and rich magnetic phase diagram depending on the doping and the applied magnetic field.

Here we report a systematic experimental and theoretical study of the insulator counterpart of the systems with tunable DMI: isostructural MnCO_3 , FeBO_3 , CoCO_3 , and NiCO_3 , with $R\bar{3}c$ crystal symmetry. In contrast to the metallic $B20$ alloys with competing long-range magnetic interactions, strongly affected by the dynamical Coulomb correlations [15], the magnetic structure of these $R\bar{3}c$ insulators is much simpler. In these systems, every metal atom interacts predominantly with its six nearest neighbors, providing a route to a truly microscopic understanding of the DMI.

The four crystals studied here have the same crystal structure [16–19], consisting in a stack of alternating $3d$ transition metal (TM) and oxygen-carbon (oxygen-boron) layers. The TM ions occupy the center of elongated MO_6 octahedra ($M \in \{\text{Mn}, \text{Fe}, \text{Co}, \text{Ni}\}$). The exchange interaction between the TM ions is mediated by the oxygen ions.

Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI.

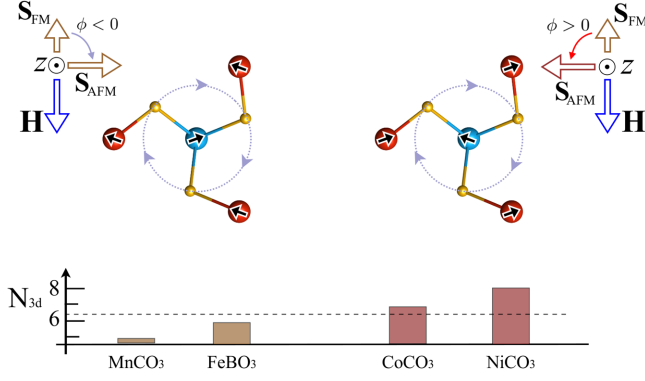


FIG. 1. Local atomic and magnetic orders in the weak ferromagnets of this work. The ions of the two magnetic sublattices are represented by blue (site 1) and red (site 2) spheres, with black arrows denoting the direction of their spins. Oxygen atoms between the two adjacent transition metal layers are represented as yellow spheres. The dotted circles highlight the twist of the oxygen layer. The bottom panel shows the occupation of the 3d level of a magnetic ion. The left and right panels show the two possible magnetic configurations which stabilize depending on the 3d occupation and, therefore, the sign of the DMI, for a net ferromagnetic moment pointing along the magnetic field \mathbf{H} . \mathbf{S}_{AFM} denotes the direction of the antiferromagnetic spin structure.

The structural twist of the oxygen layers with respect to the TM layers (Fig. 1) shifts the oxygen atoms away from the middle point between TM atoms and breaks the inversion symmetry at the oxygen sites, thus allowing the DMI interaction between the TM sites. This twist alternates in sign from one oxygen layer to the next, such that the crystal is globally centrosymmetric.

These crystals have the same antiferromagnetic order, if one ignores the small ferromagnetic component: the magnetic moments are in the basal plane, aligned parallel in a single TM layer and antiparallel between adjacent layers. However, due to the DMI, the antiferromagnetic alignment is not exactly collinear, but there is a small canting in plane, in the same direction for all the spins, resulting in a net macroscopic magnetization. The canting is a direct manifestation of the DMI, both in magnitude and in sign. The relation between DMI and ferromagnetic moment can be grasped by assuming that the single-ion anisotropy allows

the spins to rotate freely in the ab plane, and writing the classical Hamiltonian for nearest-neighbor spins as

$$\mathcal{H} = JS_1 \cdot S_2 + \mathbf{D} \cdot [\mathbf{S}_1 \times \mathbf{S}_2], \quad (1)$$

where J is the isotropic exchange constant and \mathbf{D} is known as the Dzyaloshinskii vector. The Hamiltonian minimizes energy by canting the spins with a small angle $\phi \sim \frac{1}{2} D_z / J$, where D_z is the component of \mathbf{D} parallel to the c axis. (This defines the sign $\sigma_\phi = \pm 1$ of the canting angle, which reverses from one sublattice to the other: it is chosen as equal to the sign of D_z .) The magnitude of the canting angle or, equivalently, the ratio of the net magnetization to the sublattice magnetization is of the order of a few mrad [20–24] (Table I). Remarkably, it does not vary with the temperature below the onset of magnetic order [23]. Its sign, however (or equivalently the sense of \mathbf{D}), has been determined experimentally in only a handful of weak ferromagnets [51–57], using interference effects in nuclear magnetic resonance [52,54], in polarized neutron diffraction [53,55], or in polarized x-ray diffraction [56,57]. Other methods, such as electron spin resonance [58] and spin wave spectroscopy [59–61] have been shown to be able to determine the sign of DMI in certain classes of single crystals. When a Skyrmion lattice is formed, polarized neutron small angle scattering is also used [12–14].

Diffraction experiment.—Here, we use a variation on the polarized x-ray diffraction technique employed in the case of FeBO₃ [56] to determine the sign of the canting angle in the four weak ferromagnets under consideration. For this purpose, one needs to find the sign of the antiferromagnetic spin structure factor, which for $(0, 0, 6n + 3)$ reflections is simply the difference between the spin vectors at site 1 (blue sphere in Fig. 1) and one of its nearest neighbors (site 2, red spheres), $\mathbf{S}_{\text{AFM}} = \mathbf{S}_1 - \mathbf{S}_2$. The macroscopic ferromagnetic moment can be aligned by a weak external magnetic field, which allows the entire magnetic structure to be rotated within the ab plane. While the intensity of magnetic scattering is easily determined, the all-important sign is lost when measuring the intensity of pure magnetic reflections with x rays or neutrons. We therefore exploit the interference between two x-ray amplitudes, one of magnetic origin, and a reference amplitude that is independent of the magnetic structure [56]. The former is dominated by

TABLE I. Experimental and theoretical values of the canting angle (degrees). The experimental magnitudes are taken from the literature. The experimental signs and the *ab initio* values are taken from this work. The sign of the canting angle corresponds to the sign of the DMI. N_{3d} is the number of the 3d electrons per transition metal site obtained from first-principles calculations (for details, see Supplemental Material [25]).

Compound	Magnetic ion	Z	N_{3d}	Canting angle ϕ (deg) experimental	Canting angle ϕ (deg) <i>ab initio</i>
MnCO ₃	Mn ²⁺	25	5.0	−0.04 [50], −0.4 [20,22]	−0.05
FeBO ₃	Fe ³⁺	26	5.8	−0.9 [23]	−0.8
CoCO ₃	Co ²⁺	27	7.1	4.9 [21,22]	4.7
NiCO ₃	Ni ²⁺	28	8.2	10.8 [22]	7.4

x -ray nonresonant magnetic scattering [62], while the latter is quadrupole resonant elastic x -ray scattering (REXS) [63]. More details on both amplitudes are given in Supplemental Material [25]. The interference is measured at the 009 Bragg reflection of the crystals of interest, which is forbidden for Thomson scattering (i.e., space group forbidden) but allowed for the two scattering mechanisms outlined above.

It is, perhaps, worth noting that the sign of the DMI does not affect the direction of the ferromagnetic moment as it follows the external field. Rather, it determines whether one ferromagnetically aligned sheet points to the left, and the one above it to the right, or vice versa. This difference is simply the phase of the magnetic modulation, which is encoded in the phase of the magnetic scattering.

The diffraction experiments reported here use the same setup as that described in Ref. [56]. We measured the 009 forbidden reflection of the four crystals with monochromatic x rays tuned to the K -edge resonance of their respective magnetic ion. The samples were macroscopic single crystals of high quality with a large 001 facet, except for the NiCO_3 crystal, which was a grain of a few tens of microns. The measurements were performed well below their respective Néel temperature, at 300, 7.5, 13, and 5.5 K for, respectively, FeBO_3 , MnCO_3 , CoCO_3 , and NiCO_3 . A ~ 0.01 T magnetic field, sufficient to produce a single domain state aligned with the magnet, was applied by a pair of permanent magnets rotated about the sample c axis by an angle η (see Fig. 2). The crystals were rotated by azimuthal angles ψ about the scattering vector, to suitable orientations for the measurements (see Supplemental Material for details [25]). Measurements were performed at beam line I16 of Diamond Light Source [64], using linearly polarized x rays and a linear polarization analyzer crystal to reject the scattered x rays of unrotated polarization.

As a coherent sum of two scattering amplitudes, the diffraction intensity is the sum of a pure magnetic term, a pure resonant term, and an interference term (see Supplemental Material [25]),

$$I(E, \psi, \eta) = f_m^2 \sin^2 \eta + |Q(E)|^2 \cos^2 3\psi + 2\sigma_\phi f_m \Im[Q(E)] \cos 3\psi \sin \eta, \quad (2)$$

where f_m is a known real positive quantity related to the nonresonant magnetic scattering amplitude, E is the x -ray energy, and $Q(E)$ is a complex spectroscopic term related to the REXS amplitude. The latter can be calculated with a x -ray spectroscopy software such as FDMNES [65], which was used in this work. From Eq. (2), it is clear that one can extract the sign of the DMI (σ_ϕ) by rotating the magnetic field while maintaining a fixed crystal azimuth (ψ) and x -ray energy (E). The results of such measurements are presented in Fig. 2.

The sign of the magnetic structure factor is determined by the deviation of the measured intensity toward $\eta = 90^\circ$ or $\eta = 270^\circ$, i.e., whether the red rings in Fig. 2 go up or down. The results are remarkably clear: the sign of the DMI is the same in FeBO_3 and MnCO_3 , which are both opposite to CoCO_3 and NiCO_3 . More precisely, the canting angle is negative (Fig. 1, left) in FeBO_3 and MnCO_3 , and positive (Fig. 1, right) in CoCO_3 and NiCO_3 . These signs represent the missing information from the absolute values of the canting angles that are reported in the literature (Table I) and complete our knowledge of the relative strength of the DMI in this series of materials.

A reliable model for the resonant spectrum $Q(E)$ (and, in particular, its imaginary part) is a key requisite for the correct interpretation of the scattering phase. A series of measurements at various energies and azimuths confirmed the shape of the resonance, predicted by FDMNES, and showed that the resonant amplitude just above the resonance energy has a phase that is independent of the magnetic ion ($3d$ shell filling). This seemingly complex scattering process therefore provides a robust and consistent reference wave, and a reliable interpretation of the interference data. At photon energies far below the core-level resonances the resonant term vanishes [$Q(E) \rightarrow 0$] and pure magnetic scattering is observed [the $\sin^2 \eta$ term of

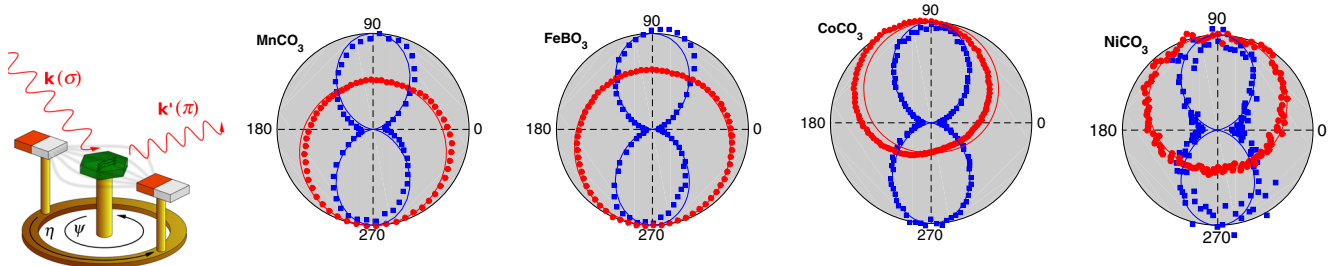


FIG. 2. X -ray diffraction experiment: schematic view and main results. Normalized experimental values of the diffraction intensity versus magnet angle η , for the series of weak ferromagnets. The blue curves are measured below the resonance energy and show the pure magnetic scattering intensity, which is symmetric and insensitive to the scattering phase. The red curves are on resonance and include a strong interference term that breaks the symmetry and gives the phase of the magnetic scattering, revealing the sign of the DMI. Experimental data (symbols) are shown with their fits (plain lines) against Eq. (2). For the off-resonance data, $Q(E) = 0$ is enforced. The deviation from the 90° – 270° symmetry axis, particularly strong in the case of CoCO_3 and not explained by Eq. (2), is discussed in Supplemental Material [25].

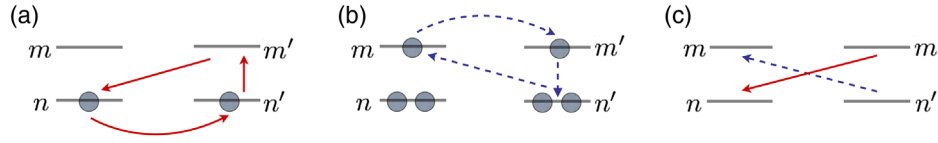


FIG. 3. Visualization of the toy tight-binding model proposed for explaining the change of DMI sign in the weak ferromagnets of this work. The filling of the energy levels in the ground state electronic configuration for $N = 2$ [(a), left] and $N = 6$ [(b), center] is shown. Arrows denote hopping (interatomic) and spin-orbit coupling (intra-atomic) excitations (between orbital states n, n', m, m') corresponding to the Dzyaloshinskii-Moriya interaction. [(c), right] Comparison of the (a) and (b) excitation processes reveals the difference in hoppings between excited and ground states.

Eq. (2)]: the data become symmetric (Fig. 2), losing all information about the scattering phase.

First-principles calculations.—To simulate the electronic structure and magnetic properties of the selected compounds we used the Vienna *ab initio* simulation package (VASP) [66,67] within local density approximation taking into account the on-site Coulomb interaction U and SOC (LDA + U + SO) [68]. All the technical details are presented in Supplemental Material [25].

Table I gives a summary of the main theoretical and experimental results. One can see that the theory reproduces the change of the DMI sign through the series of studied compounds, observed experimentally. While the absolute values of the canting angles are slightly variable depending on the U value used in the calculation, their signs turn out to be robust. Importantly, our first-principles calculations revealed that the chemical bonding in all four systems has more covalent rather than ionic character, as indicated by the deviation of the number of the 3d electrons from the pure ionic values, and magnetization of the oxygen atoms.

Toy model.—According to Hund's rules, once the electronic shell becomes more than half filled, the preferable mutual orientation of the spin and orbital moments changes. It is tempting to use this argument to explain the change of the sign of the DMI across the series of carbonates. However, the present examples all have more-than-half-filled 3d shells, and therefore parallel spin and orbital moments. We must therefore look further for an explanation of the microscopic mechanism behind the preferred magnetic chirality.

Here we propose a simple and transparent microscopic explanation of the DMI sign change in the $R\bar{3}c$ insulators, based on a minimal toy model. The first step is to express the total Dzyaloshinskii-Moriya interaction between two atoms i and j as a sum of partial interorbital contributions (IO-DMI), $\mathbf{D}_{ij} = \sum_{nn'} \mathbf{D}_{ij}^{nn'}$. Here n (n') denote the half-filled states, which are magnetic and therefore contribute to the formation of the total spin moment of each atom.

Then we analyze the IO-DMI by means of a superexchange-based approach developed by Moriya [3],

$$\mathbf{D}_{ij}^{nn'} = \frac{8i}{U} (t_{ij}^{nn'} \mathbf{C}_{ji}^{n'n} - \mathbf{C}_{ij}^{nn'} t_{ji}^{n'n}), \quad (3)$$

where $t_{ij}^{nn'}$ is the (unperturbed) hopping integral between the n th ground orbital state of i th atom and n' th orbital state of the j th atom; $\mathbf{C}_{ij}^{nn'}$ is the corresponding hopping renormalized by SOC and U is the on-site Coulomb interaction. Since $t_{ij}^{nn'} = t_{ji}^{n'n}$ and the hoppings with SOC are imaginary, the IO-DMI is nonzero if $\mathbf{C}_{ij}^{nn'} = (\mathbf{C}_{ji}^{n'n})^*$. This SOC-affected hopping integral is the quantity of interest, since it contains the information about the DMI sign. As it was shown by Moriya [3], $\mathbf{C}_{ij}^{nn'}$ is related to the transfer of the electrons (holes) between the half-filled ground states and the excited ones. The latter can be either empty or fully occupied.

Importantly, the particular electronic configuration of the excited orbital states is related to the sign and magnitude of the IO-DMI. To demonstrate this, we consider the simplest two-orbital two-site model with the different number of electrons, $N = 2$ [Fig. 3(a)] and $N = 6$ [Fig. 3(b)]. Here n and n' are the ground state orbitals in case (a), while m and m' are the ground state orbitals in case (b). We fix the hopping integrals in our consideration, which means that the geometry of the model system does not change when we vary the number of electrons.

As it follows from the experimental data and first-principles results (Table I) the DMI changes in both sign and magnitude across the series. For our toy model we found that $\mathbf{C}_{21}^{n'n} = -\mathbf{C}_{21}^{m'm}$ (see Supplemental Material [25]), simply because $\mathbf{C}_{21}^{n'n} \sim (t_{21}^{n'n} - t_{21}^{n'm})$ and $\mathbf{C}_{21}^{m'm} \sim (t_{21}^{m'm} - t_{21}^{m'n})$ [Fig. 3(c)]. It implies that $\mathbf{D}_{12}^{nn'}$ ($N = 2$) and $\mathbf{D}_{12}^{mm'}$ ($N = 6$) must have opposite signs.

As for magnitude of the DMI, it is controlled by the hopping strength between orbital states of the same symmetry, $t_{ij}^{nn'}$ and $t_{ij}^{mm'}$. From the basic electronic structure viewpoint, the higher-lying energy levels are usually the antibonding states, corresponding to a stronger metal-ligand hybridization. In our case, it leads to the following relation: $t_{ij}^{nn'} < t_{ij}^{mm'}$, which gives $|\mathbf{D}_{12}^{nn'}| < |\mathbf{D}_{12}^{mm'}|$ in agreement with the experimental observations (Table I). Thus, already at the level of the Moriya's approach, both sign and magnitude of the IO-DMI are shown to depend on the orbital's filling. By changing the occupation of the 3d states we change the balance between empty and fully occupied channels for the IO-DMI. It results in the change of sign and magnitude of the total DMI. In contrast to the previous

considerations on metals [69–71] with complex dependence of the DMI energy on the electronic structure, our toy model for insulators puts forward an intuitive picture of DMI.

To summarize, we have performed a systematic experimental and theoretical investigation of the Dzyaloshinskii-Moriya antisymmetric exchange interaction in a series of isostructural weak ferromagnets, and have discovered and explained a dramatic variation in magnitude and sign as the 3d orbitals are gradually filled. Our novel x-ray diffraction technique yields both the amplitude and phase of the magnetic diffraction, essential for determining its sign. We have shown that it is suitable even for very small (few tens of microns) crystal samples. The dramatic evolution of the Dzyaloshinskii-Moriya interaction with electron filling, and the ability of modern first-principles calculations to model it, bodes very well for a future in which the exchange interactions can be tuned for spintronics technologies, and important material properties predicted by computational methods.

The authors acknowledge Diamond Light Source for time on beam line I16 under Grants No. MT-7703 and No. MT-11751 and the XMaS facility at the European Synchrotron Radiation Facility for beamtime under Grant No. BM-28-01-966. We acknowledge fruitful communications with P. J. Brown, N. M. Kreines, Igor Solovyev, Alexander Tsirlin, and Frederic Mila, and Yves Joly for his valuable help with the FDMNES code. We are in debt to N. M. Kreines for providing the MnCO₃ and CoCO₃ single crystals. The work of V. V. M. is supported by the grant of the President of Russian Federation Grant No. MD-6458.2016.2. A. I. L. acknowledges the support of Grant No. DFG SFB-668 and the excellence cluster CUI. M. I. K. acknowledges support from ERC Advanced Grant No. 338957 FEMTO/NANO. Y. O. K. acknowledges the computational resources provided by the Swedish National Infrastructure for Computing (SNIC) and Uppsala Multidisciplinary Center for Advanced Computational Science (UPPMAX). The list of authors follows alphabetical order and is not indicative of the importance of the contribution of each.

*Corresponding author.

guillaume.beutier@simap.grenoble-inp.fr

- [1] I. Dzyaloshinsky, *J. Phys. Chem. Solids* **4**, 241 (1958).
- [2] T. Moriya, *Phys. Rev. Lett.* **4**, 228 (1960).
- [3] T. Moriya, *Phys. Rev.* **120**, 91 (1960).
- [4] M. Bode, M. Heide, K. Von Bergmann, P. Ferriani, S. Heinze, G. Bihlmayer, A. Kubetzka, O. Pietzsch, S. Blügel, and R. Wiesendanger, *Nature (London)* **447**, 190 (2007).
- [5] X. Yu, Y. Onose, N. Kanazawa, J. Park, J. Han, Y. Matsui, N. Nagaosa, and Y. Tokura, *Nature (London)* **465**, 901 (2010).
- [6] S. Heinze, K. Von Bergmann, M. Menzel, J. Brede, A. Kubetzka, R. Wiesendanger, G. Bihlmayer, and S. Blügel, *Nat. Phys.* **7**, 713 (2011).
- [7] S. X. Huang and C. L. Chien, *Phys. Rev. Lett.* **108**, 267201 (2012).
- [8] H. Katsura, N. Nagaosa, and A. V. Balatsky, *Phys. Rev. Lett.* **95**, 057205 (2005).
- [9] I. A. Sergienko and E. Dagotto, *Phys. Rev. B* **73**, 094434 (2006).
- [10] S. Emori, U. Bauer, S.-M. Ahn, E. Martinez, and G. S. Beach, *Nat. Mater.* **12**, 611 (2013).
- [11] F. J. Buijnsters, Y. Ferreiros, A. Fasolino, and M. I. Katsnelson, *Phys. Rev. Lett.* **116**, 147204 (2016).
- [12] S.-A. Siegfried, E. V. Altynbaev, N. M. Chubova, V. Dyadkin, D. Chernyshov, E. V. Moskvina, D. Menzel, A. Heinemann, A. Schreyer, and S. V. Grigoriev, *Phys. Rev. B* **91**, 184406 (2015).
- [13] S. V. Grigoriev, N. M. Potapova, S.-A. Siegfried, V. A. Dyadkin, E. V. Moskvina, V. Dmitriev, D. Menzel, C. D. Dewhurst, D. Chernyshov, R. A. Sadykov, L. N. Fomicheva, and A. V. Tsvyashchenko, *Phys. Rev. Lett.* **110**, 207201 (2013).
- [14] S. V. Grigoriev, S.-A. Siegfried, E. V. Altynbayev, N. M. Potapova, V. Dyadkin, E. V. Moskvina, D. Menzel, A. Heinemann, S. N. Axenov, L. N. Fomicheva, and A. V. Tsvyashchenko, *Phys. Rev. B* **90**, 174414 (2014).
- [15] V. V. Mazurenko, A. O. Shorikov, A. V. Lukyanov, K. Kharlov, E. Gorelov, A. I. Lichtenstein, and V. I. Anisimov, *Phys. Rev. B* **81**, 125131 (2010).
- [16] R. W. G. Wyckoff, *Am. J. Sci.* **50**, 317 (1920).
- [17] R. Diehl, *Solid State Commun.* **17**, 743 (1975).
- [18] E. Maslen, V. Streltsov, N. Streltsova, and N. Ishizawa, *Acta Crystallogr. Sect. B* **51**, 929 (1995).
- [19] F. Pertlik, *Acta Crystallogr. Sect. C* **42**, 4 (1986).
- [20] A. S. Borovik-Romanov, *Sov. Phys. JETP* **9**, 539 (1959).
- [21] A. S. Borovik-Romanov and V. I. Ozhogin, *Sov. Phys. JETP* **12**, 18 (1961).
- [22] N. M. Kreines and T. A. Shal'nikova, *Sov. Phys. JETP* **31**, 280 (1970).
- [23] M. P. Petrov, G. A. Smolensky, A. P. Paugurt, and S. A. Kizhaev, *AIP Conf. Proc.* **5**, 379 (1972).
- [24] U. Köbler, A. Hoser, J. Bos, W. Schäfer, and L. Pohlmann, *Physica B (Amsterdam)* **355**, 90 (2005).
- [25] See Supplemental Material at <http://link.aps.org/supplemental/10.1103/PhysRevLett.119.167201> details on sample growth and their magnetic characterisation, a detailed analytical framework for the diffraction experiment, and more details on the first-principle calculations and the toy model, which includes Refs. [26–49].
- [26] O. Muller, M. P. O'Horo, and J. F. O'Neill, *J. Solid State Chem.* **23**, 115 (1978).
- [27] I. Maartense, *Phys. Rev.* **188**, 924 (1969).
- [28] I. Maartense, *Phys. Rev. B* **6**, 4324 (1972).
- [29] A. S. Moskvina and M. A. Vigura, *Sov. Phys. Solid State* **28**, 1268 (1986).
- [30] T. Bither, C. G. Frederick, T. Gier, J. Weiher, and H. Young, *Solid State Commun.* **8**, 109 (1970).
- [31] R. A. Alikhanov, *Sov. Phys. JETP* **9**, 1204 (1959).
- [32] A. S. Moskvina, M. A. Vigura, and A. P. Agafonov, *Sov. Phys. Solid State* **28**, 1631 (1986).
- [33] J. Kaczer, *Sov. Phys. JETP* **16**, 1443 (1963).
- [34] V. Ozhogin, *Sov. Phys. JETP* **18**, 1156 (1964).
- [35] A. Bazhan, *Sov. Phys. JETP* **39**, 531 (1974).

- [36] D. Pincini *et al.* (to be published).
- [37] J. Brown (private communication).
- [38] M. Blume, in *Resonant Anomalous X-Ray Scattering* (Elsevier, New York, 1994), p. 495.
- [39] G. Beutier, E. Ovchinnikova, S. P. Collins, V. E. Dmitrienko, J. E. Lorenzo, J.-L. Hodeau, A. Kirfel, Y. Joly, A. A. Antonenko, V. A. Sarkisyan, and A. Bombardi, *J. Phys. Condens. Matter* **21**, 265402 (2009).
- [40] J. P. Hill and D. F. McMorrow, *Acta Crystallogr. Sect. A* **52**, 236 (1996).
- [41] V. E. Dmitrienko, E. N. Ovchinnikova, S. P. Collins, G. Nisbet, and G. Beutier, *J. Phys. Conf. Ser.* **519**, 012003 (2014).
- [42] Y. Joly, *Phys. Rev. B* **63**, 125120 (2001).
- [43] D. Treves, *J. Appl. Phys.* **36**, 1033 (1965).
- [44] M. Blume and D. Gibbs, *Phys. Rev. B* **37**, 1779 (1988).
- [45] P. E. Blöchl, *Phys. Rev. B* **50**, 17953 (1994).
- [46] G. Kresse and D. Joubert, *Phys. Rev. B* **59**, 1758 (1999).
- [47] S. L. Dudarev, G. A. Botton, S. Y. Savrasov, C. J. Humphreys, and A. P. Sutton, *Phys. Rev. B* **57**, 1505 (1998).
- [48] A. Moskvina, *J. Magn. Magn. Mater.* **400**, 117 (2016).
- [49] A. I. Liechtenstein, V. I. Anisimov, and J. Zaanen, *Phys. Rev. B* **52**, R5467 (1995).
- [50] A. Kosterov, T. Frederichs, and T. von Döbeneck, *Phys. Earth Planet. Inter.* **154**, 234 (2006).
- [51] T. Moriya, *Phys. Rev.* **117**, 635 (1960).
- [52] R. G. Shulman, *Phys. Rev.* **121**, 125 (1961).
- [53] P. J. Brown and J. B. Forsyth, *J. Phys. C* **14**, 5171 (1981).
- [54] A. S. Moskvina, *Sov. Phys. Solid State* **32**, 959 (1990).
- [55] P. J. Brown and T. Chatterji, *Phys. Rev. B* **84**, 054426 (2011).
- [56] V. Dmitrienko, E. Ovchinnikova, S. Collins, G. Nisbet, G. Beutier, Y. Kvashnin, V. Mazurenko, A. Liechtenstein, and M. Katsnelson, *Nat. Phys.* **10**, 202 (2014).
- [57] J. Kokubun *et al.* (to be published).
- [58] C. Laplane, E. Zambrini Cruzeiro, F. Fröwis, P. Goldner, and M. Afzelius, *Phys. Rev. Lett.* **117**, 037203 (2016).
- [59] Y. Iguchi, S. Uemura, K. Ueno, and Y. Onose, *Phys. Rev. B* **92**, 184419 (2015).
- [60] S. Seki, Y. Okamura, K. Kondou, K. Shibata, M. Kubota, R. Takagi, F. Kagawa, M. Kawasaki, G. Tatara, Y. Otani, and Y. Tokura, *Phys. Rev. B* **93**, 235131 (2016).
- [61] R. Takagi, D. Morikawa, K. Karube, N. Kanazawa, K. Shibata, G. Tatara, Y. Tokunaga, T. Arima, Y. Taguchi, Y. Tokura, and S. Seki, *Phys. Rev. B* **95**, 220406 (2017).
- [62] F. de Bergevin and M. Brunel, *Acta Crystallogr. Sect. A* **37**, 314 (1981).
- [63] S. Grenier and Y. Joly, *J. Phys. Conf. Ser.* **519**, 012001 (2014).
- [64] S. P. Collins, A. Bombardi, A. R. Marshall, J. H. Williams, G. Barlow, A. G. Day, M. R. Pearson, R. J. Woolliscroft, R. D. Walton, G. Beutier, and G. Nisbet, *AIP Conf. Proc.* **1234**, 303 (2010).
- [65] Y. Joly, O. Bunău, J. E. Lorenzo, R. M. Galéra, S. Grenier, and B. Thompson, *J. Phys. Conf. Ser.* **190**, 012007 (2009).
- [66] G. Kresse and J. Hafner, *Phys. Rev. B* **47**, 558 (1993).
- [67] G. Kresse and J. Furthmüller, *Phys. Rev. B* **54**, 11169 (1996).
- [68] I. V. Solovyev, A. I. Liechtenstein, and K. Terakura, *Phys. Rev. Lett.* **80**, 5758 (1998).
- [69] A. Fert and P. M. Levy, *Phys. Rev. Lett.* **44**, 1538 (1980).
- [70] V. Kashid, T. Schena, B. Zimmermann, Y. Mokrousov, S. Blügel, V. Shah, and H. G. Salunke, *Phys. Rev. B* **90**, 054412 (2014).
- [71] A. Belabbes, G. Bihlmayer, F. Bechstedt, S. Blügel, and A. Manchon, *Phys. Rev. Lett.* **117**, 247202 (2016).